

# Study of liquid-liquid equilibria in aqueous two-phase systems formed by poly (ethylene glycol) (PEG) and sodium thiosulfate pentahydrate ( $\text{Na}_2\text{S}_2\text{O}_3 \cdot 5\text{H}_2\text{O}$ ) at different temperatures

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## ABSTRACT

This study aimed at providing experimental liquid-liquid equilibrium (LLE) data for aqueous two-phase systems (ATPSs) formed by poly (ethylene glycols) (PEG) of different molecular weights (1500 or 4000 or 6000)  $\text{g}\cdot\text{mol}^{-1}$  and sodium thiosulfate pentahydrate at different temperatures (293.15–313.15) K and under atmospheric pressure. Correlations of experimental data of binodal curves were carried out using the Merchuk methodology. The effects of temperature, polymer molecular weight and of the nature of the anion of salts on binodal curves were discussed. In comparison with other anions previously investigated, the salting-out ability of the thiosulfate anion was between those of citrate and tartrate anions. Finally, the Othmer-Tobias and Bancroft equations and the NRTL activity coefficient model were used for correlating tie line compositions.

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## 1. Introduction

Aqueous two-phase systems (ATPSs) can be obtained through the combination of two water-soluble polymers with different chemical structures [1,2] or a polymer and a salt [3,4] or, according to recent findings, by mixing an ionic liquid and a salt [5,6], wherein the salt used can be either organic or inorganic in both cases.

ATPSs were discovered in 1896, when Beijerinck [7] mixed aqueous solutions of either starches and gelatin or agar-agar and gelatin. Such mixture formed a turbid system that formed two phases spontaneously while resting, in which the upper phase was rich in gelatin and the lower phase in starch or agar-agar [8]. Additional studies were conducted by Ostwald and Hertel in 1929, showing that starches from different sources provided diagrams with different phase compositions and, therefore, variations in molecular interactions influenced compositions of the phases in balance. In the late 40s, Dobry and Boyer-Kawenoki showed separation of phases is also obtained when various types of polymers

are combined [9,10].

Around the 60s, Albertson [11,12] applied the ATPS formed by poly (ethylene glycol) and dextran in a separation process or biological partition. From this, knowledge of new ATPSs and its application in purification processes have been well explored by researchers. Since studies of Gutowski and his collaborators (2003) [5], ATPSs composed of ionic liquids and salts were also published [13,14], despite their higher costs compared with aqueous systems composed of PEG and Salt [15].

The use of ATPSs in the separation and purification of biomolecules (proteins, enzymes, cells, among others), shows advantages in relation to conventional methods, such as cost reduction, minimization of separation stages and high purification of products. Furthermore, this type of system presents a diversity of application areas, for example, extractive fermentations, determination of solute surface properties, and characterization of ligand-nucleic acid binding [15,16]. The literature mentions several liquid-liquid equilibrium data for (PEG-sodium sulfate) ATPSs [17–22], but no data is available for (PEG + sodium thiosulfate + water) systems. Also, only one set of data for (polyethylene oxide + sodium thiosulfate) ATPS was reported [23].

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In this study, aqueous two-phase systems composed of PEG (1500, 4000 and 6000 g mol<sup>-1</sup>) + sodium thiosulfate pentahydrate were determined at three different temperatures  $T = (293.15, 303.15 \text{ and } 313.15) \text{ K}$  with  $u(T) = 0.05$  and under atmospheric pressure. The correlations of Othmer-Tobias [24] and Bancroft [25] were used to verify the quality of tie lines obtained from all systems. Quantification of the composition of the tie lines was achieved using the method of Merchuk et al. [26] and following the procedure used by Homrich et al. [27] for calculating standard uncertainties in mass fractions through error propagation. The effects of temperature and polymer molecular weight on the LLE were analyzed.

## 2. Experimental

### 2.1. Chemical reagents

Table 1 lists the compounds used in this study and their characteristics (IUPAC (International Union of Pure and Applied) names, CAS Registry numbers, suppliers and purities in mass fraction). PEGs were standard analytical grade. The number of water molecules of sodium thiosulfate pentahydrate in the aqueous solutions was considered. All chemicals were used as received, without any further purification. <http://www.synth.com.br/>

### 2.2. Experimental procedure

The phase equilibrium diagrams were obtained by turbidimetry at  $T = (293.15, 303.15 \text{ and } 313.15) \text{ K}$  with  $u(T) = 0.05 \text{ K}$ , according to the methodology described by Albertsson (1986) [12]. Aqueous solutions of salt at 35% (m/m) and PEG at 50% (m/m) were prepared in equilibrium glass cells connected to a thermostatic bath (Tecnal, model TE-184). The PEG solution was carefully titrated with the salt solution until a cloud point was noted (biphasic region), and the system composition was then registered. After that, a known mass of distilled water was added until the solution turned limpid (single-phase region). Alternating several times between titration with salt solution or distilled water while keeping the system under stirring using a magnetic stirrer (Fisatom, Model 752), identifying the biphasic region was possible. Compositions of ternary systems were determined through mass quantification of all the components, using an analytical balance (Shimadzu, model AX200), accurate to  $\pm 0.0001 \text{ g}$ .

The tie lines were determined by the gravimetric method, originally proposed by Merchuk et al. [26] through the application of the lever-arm rule for the relation between the mass composition in the upper phase and the system global composition. Ternary mixtures (around 5 g) within the two-phase region composed of PEG, salt and water, were prepared in small glass tubes (9 mL, approx.). Each prepared solution was vigorously stirred for 10 min at 2500 rpm in a vortex (Heldolph, type REAX control). After that, each tube was put into a thermostatic bath at a constant temperature for at least 12 h. Then, both upper and lower phases were carefully separated and weighted. For determination of tie line compositions, a system of four equations (Eqs. (1)–(4)) and

four unknowns ( $w_1^I$ ,  $w_2^I$ ,  $w_1^{II}$  and  $w_2^{II}$ ) were solved. Equations (1) and (2) correspond to experimental binodal curves, and equations (3) and (4) are related to the lever-arm rule [26]:

$$w_1^I = A \cdot \exp\left(B(w_2^I)^{0.5} - C(w_2^I)^3\right) \quad (1)$$

$$w_1^{II} = A \cdot \exp\left(B(w_2^{II})^{0.5} - C(w_2^{II})^3\right) \quad (2)$$

$$w_1^I = \frac{w_1^M}{\alpha} - \left(\frac{1-\alpha}{\alpha}\right) w_1^{II} \quad (3)$$

$$w_2^I = \frac{w_2^M}{\alpha} - \left(\frac{1-\alpha}{\alpha}\right) w_2^{II} \quad (4)$$

in which  $w_1$  is the mass fraction of PEG,  $w_2$  is the mass fraction of salt, superscripts “I”, “II” and  $M$  denote, respectively, the upper phase, the lower phase and the initial mixture,  $A$ ,  $B$ , and  $C$  are regressed parameters from experimental data of the binodal curve, and  $\alpha$  is the ratio between the mass in grams of the upper phase and the total mass of the mixture.

The tie-line length,  $TLL$ , and slope of the tie line,  $S$ , at different compositions were also calculated using Eqs. (5) and (6), respectively, as follows:

$$TLL = \sqrt{(w_1^I - w_1^{II})^2 + (w_2^I - w_2^{II})^2} \quad (5)$$

$$S = \frac{w_1^I - w_1^{II}}{w_2^I - w_2^{II}} \quad (6)$$

The quality of the LLE data was verified by the semi-empirical equations of Othmer-Tobias [24] (Eq. (7)) and Bancroft [25] (Eq. (8)):

$$\frac{1 - w_1^I}{w_1^I} = k_1 \left( \frac{1 - w_2^{II}}{w_2^{II}} \right)^n \quad (7)$$

$$\frac{w_3^{II}}{w_2^{II}} = k_2 \left( \frac{w_3^I}{w_1^I} \right)^r \quad (8)$$

in which  $k_1$ ,  $n$ ,  $k_2$  and  $r$  are fitting parameters.

## 3. Results and discussion

### 3.1. Binodal curves

Experimental data from binodal curves obtained at temperatures of  $T = (293.15\text{--}313.15) \text{ K}$  with  $u(T) = 0.05 \text{ K}$  under atmospheric pressure for all systems formed through the combination of the three PEGs (1500, 4000 or 6000) with sodium thiosulfate pentahydrate are given in Table 2 and represented graphically in Fig. 1.

**Table 1**

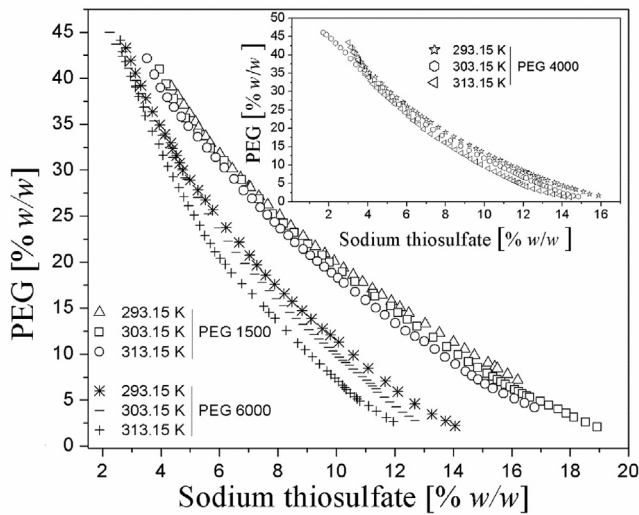
Source and purity of the chemicals used in this study.

Compounds	IUPAC NAME	CAS Registry No.	Supplier	Purity (mass fraction)
PEG 1500	Poly (ethylene glycol) 1500	25322-68-3	Synth	—
PEG 4000	Poly (ethylene glycol) 4000	25322-68-3	Synth	—
PEG 6000	Poly (ethylene glycol) 6000	25322-68-3	Synth	—
Sodium thiosulfate Pentahydrate	Sodium sulfurothioate Hydrate	10102-17-7	Synth	0.995

**Table 2**  
Experimental (Liquid + Liquid) Equilibrium Mass Fractions (w) on the Binodal curves for (PEG (1) + Sodium Thiosulfate (2) + water (3)) at different temperatures and pressure  $p = 0.094 \text{ MPa}^a$ .

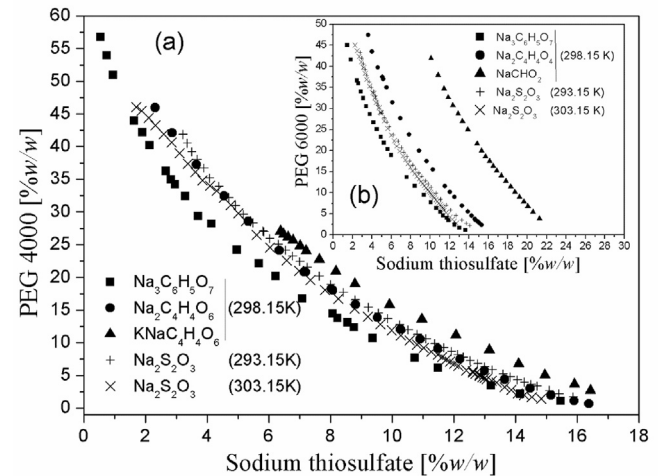
293.15 K				303.15 K				313.15 K			
100 w <sub>1</sub>	100 w <sub>2</sub>	100 w <sub>1</sub>	100 w <sub>2</sub>	100 w <sub>1</sub>	100 w <sub>2</sub>	100 w <sub>1</sub>	100 w <sub>2</sub>	100 w <sub>1</sub>	100 w <sub>2</sub>	100 w <sub>1</sub>	100 w <sub>2</sub>
<b>PEG 1500</b>											
39.06	4.36	18.57	10.57	40.94	3.95	10.77	13.78	42.15	3.52	18.84	9.84
38.08	4.57	17.84	10.90	39.36	4.19	9.93	14.17	40.41	3.77	18.30	10.05
37.10	4.78	17.11	11.23	37.78	4.44	9.16	14.53	38.98	3.98	17.76	10.26
36.17	4.98	16.42	11.55	35.64	4.85	8.51	14.84	37.91	4.22	16.78	10.64
35.25	5.18	15.73	11.88	34.00	5.28	7.89	15.16	36.85	4.45	15.88	11.00
34.64	5.29	15.08	12.17	32.35	5.70	7.53	15.36	35.82	4.70	15.03	11.35
33.66	5.53	14.43	12.48	31.01	6.17	7.22	15.51	34.79	4.94	14.27	11.66
32.94	5.68	13.27	13.04	28.94	6.77	6.96	15.63	33.61	5.26	13.36	12.02
31.78	6.01	12.28	13.52	26.86	7.37	6.67	15.79	32.43	5.58	12.51	12.37
30.59	6.29	11.30	14.01	25.22	7.83	6.39	15.95	31.39	5.87	11.95	12.69
30.14	6.44	10.53	14.39	24.21	8.20	6.13	16.11	30.25	6.17	11.39	13.01
29.18	6.72	9.85	14.72	23.20	8.56	5.90	16.24	29.03	6.50	10.54	13.37
28.22	6.99	9.05	15.18	21.96	9.04	5.68	16.37	27.80	6.83	9.69	13.72
28.17	7.02	8.60	15.41	20.71	9.52	5.45	16.51	26.90	7.12	8.90	14.07
28.12	7.05	8.40	15.51	19.96	9.77	5.29	16.62	25.93	7.40	8.12	14.42
27.16	7.35	7.77	15.85	18.92	10.21	5.29	16.62	25.15	7.64	7.68	14.63
26.20	7.65	7.14	16.20	17.88	10.64	4.84	16.99	24.34	7.89	7.24	14.84
25.06	8.05			16.58	11.26	4.42	17.27	23.61	8.09	6.76	15.09
23.92	8.44			16.26	11.33	4.01	17.59	22.89	8.36	6.28	15.35
22.81	8.86			15.20	11.87	3.55	17.86	22.14	8.58	5.72	15.72
21.69	9.28			14.49	12.11	3.10	18.13	21.41	8.87	5.15	16.09
20.90	9.60			13.75	12.44	2.57	18.53	20.74	9.11	4.67	16.44
20.11	9.92			13.02	12.77	2.04	18.92	20.10	9.35	4.20	16.78
19.34	10.24			11.79	13.32			19.47	9.59		
<b>PEG 4000</b>											
41.85	3.21	9.88	11.38	46.04	1.69	9.19	11.02	43.41	2.99	17.25	7.60
40.53	3.36	9.24	11.67	45.50	1.87	8.65	11.26	42.07	3.12	16.14	7.93
39.20	3.50	8.68	11.92	44.37	2.10	8.17	11.47	40.35	3.35	15.12	8.24
38.02	3.67	8.19	12.12	43.24	2.33	7.80	11.61	39.27	3.45	14.25	8.51
36.70	3.89	7.80	12.31	41.94	2.59	7.44	11.75	40.74	3.24	13.31	8.80
35.17	4.08	7.78	12.30	40.65	2.84	7.10	11.88	38.19	3.55	12.48	9.08
33.88	4.38	7.76	12.29	39.01	3.11	6.77	12.01	37.01	3.70	11.77	9.29
32.17	4.71	7.28	12.53	37.38	3.38	6.48	12.14	38.31	3.54	10.90	9.56
30.98	4.92	6.80	12.77	36.11	3.61	5.81	12.40	38.44	3.53	10.19	9.80
29.65	5.18	6.32	13.00	34.85	3.85	5.66	12.61	38.68	3.50	9.11	10.20
28.34	5.49	5.85	13.25	34.04	4.08	5.45	12.61	32.06	4.26	8.28	10.50
26.99	5.84	5.23	13.60	33.23	4.31	5.26	12.69	33.94	4.06	7.60	10.75
25.96	6.03	4.75	13.83	32.17	4.54	5.10	12.83	35.82	3.85	7.02	10.97
27.07	5.81	4.34	14.06	31.10	4.76	4.96	12.84	34.86	3.94	6.53	11.17
25.03	6.31	3.99	14.28	29.84	5.01	4.76	12.93	33.89	4.03	6.10	11.33
24.16	6.54	3.65	14.51	28.57	5.25	4.60	13.00	32.97	4.15	5.66	11.49
23.28	6.77	3.37	14.70	26.50	5.60	4.44	13.07	32.06	4.26	5.25	11.67
22.43	7.01	2.71	15.09	24.54	6.03	4.19	13.22	31.04	4.46	5.26	11.70
21.57	7.24	2.16	15.41	22.60	6.57	3.94	13.38	30.02	4.66	5.06	11.76
20.22	7.63	1.72	15.87	21.03	6.98	3.94	13.38	29.15	4.85	4.77	11.87
18.94	8.00			19.62	7.35	3.25	13.63	28.28	5.05	4.47	12.00
17.72	8.42			18.09	7.82	2.77	13.86	27.49	5.21	4.14	12.15
16.59	8.80			16.72	8.25	2.29	14.07	26.70	5.38	3.58	12.49
15.41	9.23			15.23	8.77	2.00	14.28	25.35	5.70	3.02	12.82
14.51	9.56			13.98	9.21	1.72	14.53	24.22	5.93	2.50	13.19
13.71	9.85			12.87	9.62	1.45	14.83	23.14	6.12	2.09	13.51
12.74	10.24			11.92	9.98			22.12	6.33	1.77	13.86
11.98	10.52			11.13	10.27			21.08	6.60	1.49	14.12
11.27	10.82			10.37	10.56			19.85	6.87	1.29	14.39
10.61	11.10			9.74	10.80			18.53	7.22		
<b>PEG 6000</b>											
43.31	2.80	12.08	9.80	45.00	2.24	14.54	8.40	44.13	2.61	14.54	7.70
41.93	2.97	11.31	10.08	43.68	2.45	13.87	8.62	42.85	2.68	13.88	7.90

<sup>a</sup> Standard uncertainties u are  $u(T) = 0.05 \text{ K}$ ,  $u(w) = 0.0001$ , and  $u(P) = 0.5 \text{ kPa}$ .



**Fig. 1.** Effect of temperature and type of PEG on binodal curves for the systems composed of PEG (1) + Sodium Thiosulfate (2) + water (3) ATPSs under atmospheric pressure.

The literature reports that increasing temperature, biphasic region in some ATPSs of the type PEG-salt is extended [28,29]. This relationship between temperature and two-phase region size is associated with the endothermic nature of the phase-separation process. In Fig. 1, an increase in temperature induces a subtle variation in solubility curves (or an increase in the size of the two-phase region), which is not statistically significant [30]. However, at higher polymer concentrations, this effect is not well defined, corroborating with Zafarani-Moattar and coworkers [31,32], who observed that, in some ATPSs formed by PEG-salt, temperature effect is undefined and, sometimes, inverted in regions where binodal curves are richer in PEG. In these regions, the intensity of the interactions between PEG molecules is responsible for phase separation, and the expectation is that decreasing temperature will cause the formation of two-phases due to an increased repulsion between PEG molecules [32]. According to Zafarani-Moattar and Sadeghi (2001) [32], in salt-rich regions, the behavior of the binodal curves under a variation in temperature depends mainly on the kind of the salt used. The behavior of these systems in this other region may be due to the different solvation properties of the salt



**Fig. 2.** Effect of salt anions on binodal curves for the systems composed of PEG 4000 (or PEG 6000) (1) + Salt (2) + water (3) ATPSs under atmospheric pressure: (a) salts: sodium citrate ( $\text{Na}_3\text{C}_6\text{H}_5\text{O}_7$ ), sodium tartrate ( $\text{Na}_2\text{C}_4\text{H}_4\text{O}_6$ ), sodium potassium tartrate ( $\text{KNaC}_4\text{H}_4\text{O}_6$ ), sodium thiosulfate ( $\text{Na}_2\text{S}_2\text{O}_3$ ) (this study); (b) salts: sodium citrate ( $\text{Na}_3\text{C}_6\text{H}_5\text{O}_7$ ), sodium succinate ( $\text{Na}_2\text{C}_4\text{H}_4\text{O}_4$ ), sodium formate ( $\text{NaCHO}_2$ ), sodium thiosulfate ( $\text{Na}_2\text{S}_2\text{O}_3$ ) (this study).

ions at different temperatures.

The effect of PEG molecular weight in the size of the biphasic region was as expected [11,12]. An increase in molecular weight of PEG promotes an increase in the biphasic region due to a reduction of the solubility of PEG in water [33], being less pronounced or even inverted between PEGs 4000 and 6000, in PEG-rich regions, concurring with results of Zhang et al. [34] for PEGs 1000 e 2000. This behavior has already been shown in the literature [35] and may be attributed to the incompatibility between the system components, due to an increase in the hydrophobicity of PEGs of higher molecular weights. In this way, the phase splitting is achieved at lower concentrations of PEGs of higher molecular weights, which tends to lower its water absorption capacity. The effect of PEG molecular weight in binodal curves is depicted in Fig. 1 and in Figure S4 in the Supplementary Material. As noted, systems formed by PEGs of higher molecular weight have greater ability to form two-phases, which suggests that they may be somewhat better for separation of biomolecules [36].

In order to correlate LLE data in terms of mass fractions, the

**Table 3**

Values of parameters of Eqs. (1) and (2), their standard deviations (sd) and coefficients of determination (*R-square*) for systems containing PEG (1) + sodium thiosulfate (2) + water (3) at different temperatures.

T/K	A (95% C.B.) <sup>b</sup>	B (95% C.B.) <sup>b</sup>	C (95% C.B.) <sup>b</sup>	R <sup>2</sup>	sd <sup>a</sup>
<b>PEG 1500</b>					
293.15	1.0786 (1.0445, 1.1126)	−4.8246 (−4.9604, −4.6887)	167.4698 (158.5552, 176.3843)	0.9996	0.0019
303.15	0.9325 (0.8852, 0.9799)	−4.1830 (−4.4026, −3.9634)	245.7538 (232.7616, 258.7460)	0.9989	0.0038
313.15	0.9595 (0.9351, 0.9840)	−4.4024 (−4.5175, −4.2872)	264.1662 (254.8999, 273.4324)	0.9996	0.0021
<b>PEG 4000</b>					
293.15	1.1407 (1.0937, 1.1878)	−5.6245 (−5.8243, −5.4248)	393.6823 (372.8304, 414.5341)	0.9993	0.0031
303.15	0.8233 (0.7951, 0.8517)	−4.2188 (−4.4120, −4.0256)	623.3137 (593.8675, 652.7599)	0.9988	0.0049
313.15	1.3505 (1.2661, 1.4350)	−6.5819 (−6.9075, −6.2562)	603.2373 (555.3699, 651.1046)	0.9988	0.0048
<b>PEG 6000</b>					
293.15	1.1370 (1.0780, 1.1952)	−5.7664 (−6.0318, −5.5009)	514.4199 (473.3316, 555.5082)	0.9991	0.0037
303.15	1.0219 (0.9805, 1.0633)	−5.3086 (−5.5282, −5.0890)	692.4398 (655.5115, 729.3680)	0.9990	0.0040
313.15	1.3902 (1.3254, 1.4549)	−7.0865 (−7.3414, −6.8316)	736.0536 (687.0734, 785.0338)	0.9992	0.0037

<sup>a</sup>  $Sd = ((\sum_{i=1}^n (100w_i^{cal} - 100w_i^{exp}))^2 / n)^{0.5}$  in which *n* is the number of binodal data.  $w_i^{exp}$  is the experimental mass fraction of PEG and  $w_i^{cal}$  is the calculated mass fraction of PEG.

<sup>b</sup> 95% C.B. = 95% confidence bounds.

**Table 4**  
Experimental (liquid-liquid) equilibrium mass fractions  $w$  for tie lines length (TLL) and slope of the tie lines ( $S$ ) for systems formed by PEG (1) + Sodium Thiosulfate Pentahydrate (2) + water (3) at different temperatures and Pressure  $p = 0.094$  MPa<sup>a</sup>.

TL	Global composition		Top phase: PEG-rich phase				Bottom phase: salt-rich phase				TLL	S
	100 $w_1$	100 $w_2$	100 $w_1$	$u(w_1)$	100 $w_2$	$u(w_2)$	100 $w_1$	$u(w_1)$	100 $w_2$	$u(w_2)$		
PEG 1500												
T = 293.15 K												
1	17.96	12.08	27.70	0.17	7.22	0.42	4.25	0.20	18.92	0.48	26.20	−2.00
2	18.01	13.38	32.38	0.11	5.87	0.37	2.05	0.12	21.72	0.41	34.22	−1.91
3	17.99	14.65	37.65	0.06	4.61	0.30	1.32	0.05	23.16	0.26	40.80	−1.96
4	17.97	15.95	42.46	0.03	3.67	0.24	0.83	0.02	24.55	0.17	46.57	−1.99
T = 303.15 K												
1	17.97	12.07	31.07	0.50	6.19	0.89	2.96	0.58	18.82	0.94	30.82	−2.23
2	18.04	13.42	36.43	0.18	4.77	0.63	1.25	0.16	21.32	0.58	38.88	−2.13
3	18.02	14.68	40.05	0.08	3.94	0.53	0.58	0.06	23.18	0.42	43.90	−2.05
4	18.00	15.91	44.47	0.04	3.07	0.46	0.32	0.03	24.49	0.31	49.07	−2.06
T = 313.15 K												
1	17.98	12.78	37.43	0.08	4.36	0.31	1.74	0.10	19.80	0.37	38.89	−2.31
2	17.51	14.27	42.11	0.05	3.41	0.28	0.86	0.06	21.61	0.31	45.09	−2.27
3	18.02	15.26	45.26	0.03	2.86	0.24	0.41	0.02	23.27	0.21	49.28	−2.20
4	17.94	16.53	48.48	0.01	2.38	0.21	0.20	0.01	24.74	0.15	53.21	−2.16
PEG 4000												
T = 293.15 K												
1	18.00	9.50	25.17	0.12	6.31	0.38	1.82	0.27	16.72	0.86	25.56	−2.24
2	17.99	10.91	30.76	0.05	5.02	0.32	0.70	0.07	18.89	0.44	33.10	−2.17
3	17.95	11.53	33.79	0.03	4.42	0.28	0.54	0.03	19.41	0.28	36.47	−2.22
4	17.97	14.04	40.44	0.01	3.31	0.23	0.09	0.01	22.58	0.19	44.72	−2.09
T = 303.15 K												
1	18.07	10.25	31.35	0.05	4.60	0.33	0.43	0.07	17.75	0.44	33.61	−2.35
2	18.06	11.50	35.84	0.02	3.62	0.30	0.13	0.02	19.45	0.30	39.06	−2.25
3	17.95	12.73	39.41	0.01	2.92	0.27	0.04	0.01	20.91	0.23	43.29	−2.19
4	18.02	14.03	42.18	0.00	2.45	0.25	0.01	0.00	22.67	0.18	46.77	−2.09
T = 313.15 K												
1	18.01	12.78	37.43	0.06	4.36	0.40	1.74	0.07	19.80	0.45	38.89	−2.31
2	18.00	14.27	42.11	0.02	3.41	0.34	0.86	0.02	21.61	0.30	45.09	−2.27
3	18.00	15.26	45.26	0.01	2.86	0.30	0.41	0.01	23.27	0.23	49.28	−2.20
4	18.04	16.53	48.48	0.00	2.38	0.28	0.20	0.00	24.74	0.19	53.21	−2.16
PEG 6000												
T = 293.15 K												
1	18.01	8.93	25.56	0.14	5.82	0.44	1.57	0.31	15.71	0.96	25.95	−2.43
2	18.00	10.19	31.57	0.07	4.57	0.38	0.70	0.09	17.36	0.49	33.42	−2.41
3	18.01	11.48	36.24	0.03	3.75	0.33	0.27	0.03	19.01	0.33	39.07	−2.36
4	17.63	12.48	38.86	0.01	3.34	0.31	0.14	0.01	20.02	0.26	42.15	−2.32
T = 303.15 K												
1	18.09	10.15	33.80	0.04	4.00	0.30	0.36	0.05	17.09	0.34	35.91	−2.56
2	18.07	11.51	37.18	0.01	3.43	0.27	0.08	0.01	19.12	0.26	40.28	−2.36
3	18.06	12.76	41.04	0.00	2.85	0.25	0.02	0.00	20.54	0.20	44.67	−2.32
4	17.96	14.00	40.50	0.00	4.00	0.28	0.00	0.00	22.83	0.22	44.66	−2.15
T = 313.15 K												
1	18.04	10.18	33.58	0.03	4.19	0.27	0.48	0.04	16.93	0.30	35.47	−2.60
2	18.05	11.45	38.25	0.01	3.52	0.23	0.18	0.01	18.42	0.19	40.88	−2.56
3	17.99	12.39	41.39	0.00	3.13	0.19	0.09	0.00	19.49	0.13	44.42	−2.52
4	18.05	13.37	43.56	0.00	2.88	0.17	0.03	0.00	20.77	0.10	47.07	−2.43

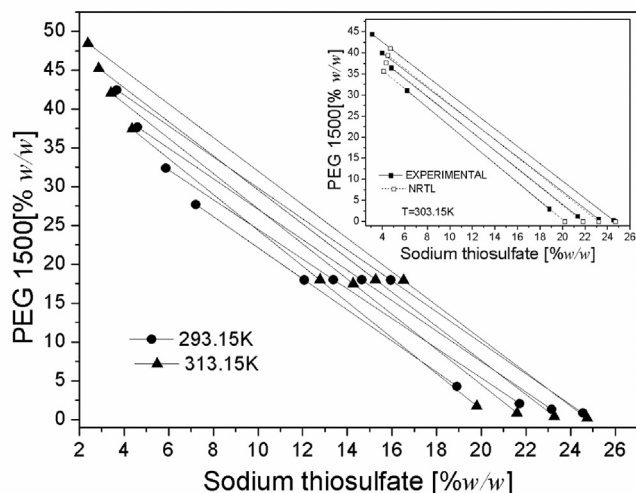
<sup>a</sup> Standard uncertainties are  $u(T) = 0.05$  K,  $u(p) = 10$  kPa  $u(w_i) < 0.9$ , for  $i = 1$  or  $2$  in total composition.

values of parameters of Eqs. (1) and (2) were obtained through a nonlinear regression (least-square method) using data of Table 2. Table 3 shows regressed values for all systems, coefficients of determination,  $R$ -square (higher than 0.99), and standard deviations,  $sd$  (lower than 0.0049), indicating a good representation of data.

Salting-out ability can be related to the Gibbs energy of hydration of ions ( $\Delta G_{hyd}$ ) [37]. Thus, we compared the salting-out ability of anion, studied in the ATPSs of this study, with other anions of

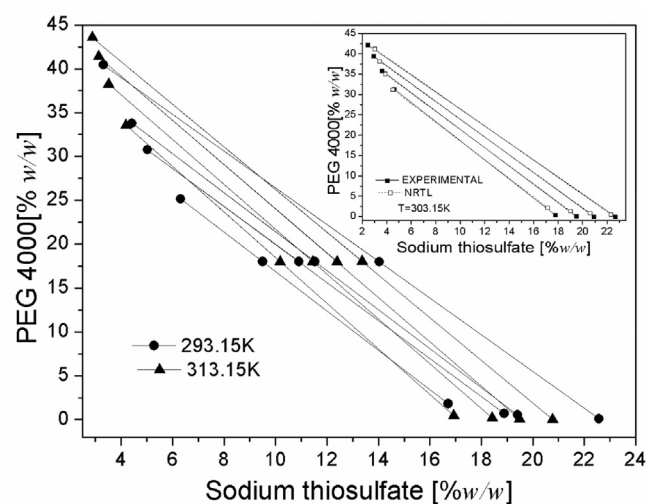
sodium salts analyzing the phase diagrams together with ( $\Delta G_{hyd}$ ) values. So, ATPSs involving PEG 4000 (or PEG 6000) and these salts at 298.15 K were found in the literature [37–41] and compared with systems obtained in this study at 293.15 and 303.15 K, even though our data were obtained at different temperatures. Firstly, the estimated values of ( $\Delta G_{hyd}$ ) calculated with the procedure described by Marcus [42], and reported in the literature [39,43,44], were considered in this analysis. Fig. 2 shows clearly that for salts that share a common cation but contain different anions, salting-out



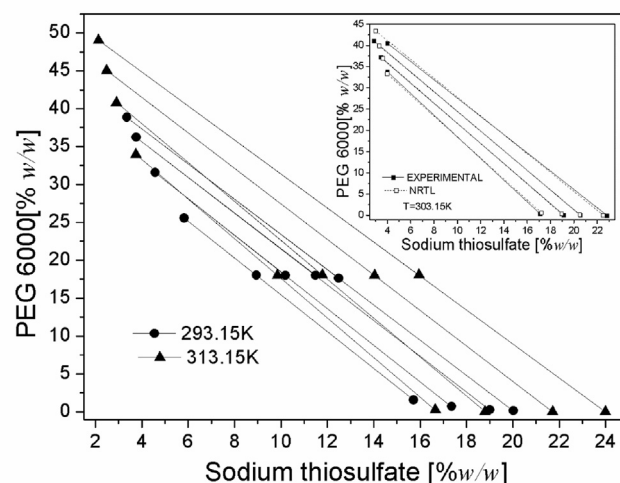


**Fig. 3.** Liquid-liquid equilibria at different temperatures for the systems composed of PEG 1500 (1) + Sodium Thiosulfate (2) + water (3) ATPSs under atmospheric pressure.

ability of anions follows the sequence (numbers in parentheses are the Gibbs energy of hydration of ions):  $C_6H_5O_7^{3-}$  ( $-2793 \text{ kJ mol}^{-1}$ ) [43]  $> S_2O_3^{2-}$  ( $-1160 \text{ kJ mol}^{-1}$ ) [44]  $> C_4H_4O_6^{2-}$  ( $-1010 \text{ kJ mol}^{-1}$ ) [44]  $> CHO^{2-}$  ( $-395 \text{ kJ mol}^{-1}$ ) [39]. Secondly, in order to evaluate the effectiveness in the phases formation of sodium potassium tartrate and include it in the above sequence, analyzing the ( $\Delta G_{hyd}$ ) of the cations  $K^+$  and  $Na^+$  was necessary. Marcus et al. [42] also reported experimental values of ( $\Delta G_{hyd}$ ) for cations  $K^+$  and  $Na^+$  as  $-295 \text{ kJ mol}^{-1}$  and  $-365 \text{ kJ mol}^{-1}$ , respectively. Considering that the negative value of the ( $\Delta G_{hyd}$ ) of  $K^+$  is lower than that of  $Na^+$ , the expectation is that the salting out ability of the di-sodium tartrate salt would be higher than that of sodium potassium tartrate. Therefore, the final sequence for the salting-out ability of the anion in Fig. 2(a) and (b) is:  $C_6H_5O_7^{3-}$  (citrate)  $> S_2O_3^{2-}$  (thiosulfate)  $> C_4H_4O_6^{2-}$  (tartrate)  $> KC_4H_4O_6^{2-}$  (Ktartrate)  $> C_4H_4O_4^{2-}$  (succinate)  $> CHO^{2-}$  (formate). In this way, the best salting-out effect in Fig. 2(a) and (b) is observed for ATPSs with sodium citrate that presented a more negative ( $\Delta G_{hyd}$ ) value. These results are in accordance with those from Li et al. [45], which showed that the salting-out effect of citrate, tartrate and succinate ions follows the



**Fig. 4.** Liquid-liquid equilibria at different temperatures for the systems composed of PEG 4000 + Sodium Thiosulfate (2) + water (3) ATPSs under atmospheric pressure.



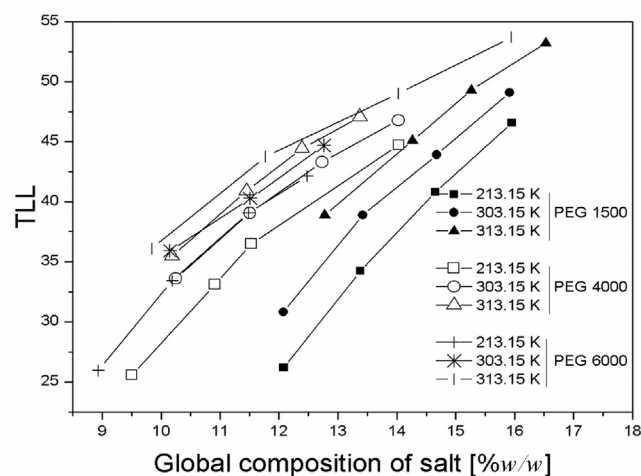
**Fig. 5.** Liquid-liquid equilibria at different temperatures for the systems composed of PEG 6000 + Sodium Thiosulfate (2) + water (3) ATPSs under atmospheric pressure.

order:  $C_6H_5O_7^{3-} > C_4H_4O_6^{2-} > C_4H_4O_4^{2-}$ . The position of binodal curves of this study in Fig. 2(a) and (b), when compared with others of the literature, agrees with the values of ( $\Delta G_{hyd}$ ) found.

### 3.2. Tie line data and correlation

Compositions of equilibrium phases, length ( $TLL$ ) and slope ( $S$ ) of the tie lines are given in Table 4. The semi-empirical tests of Othmer-Tobias [24] and Bancroft [25] agreed well with the tie-line data and presented coefficients of determination ( $R$ -square) higher than 0.97 for all systems.

According to the results in Table 3 and in Figs. 3–5, for all ATPSs, with an increase in temperature, the tie lines became more sloped, following the behavior of other PEG-salt systems [46–48]. No remarkable effect of PEG molecular weight was revealed in the tie line slopes. For the sake of clearness, Figs. 3–5 show the calculated tie lines with the NRTL model at 303.15 K only. Fig. 6 shows higher amounts of salt in initial ternary mixture (global composition) are related to greater  $TLL$  values for all PEG-salt systems independently



**Fig. 6.** Tie line length versus global composition of salt for PEG (1) + Sodium Thiosulfate (2) + water (3) ATPSs at different temperatures and under atmospheric pressure.

**Table 5**

Binary interaction parameters of the NRTL equation, and correlation performance for the system used in this study.

<i>i/j</i>	<sup>a</sup> <i>A</i> <sub>0ij</sub> /K	<sup>a</sup> <i>A</i> <sub>0ji</sub> /K	<sup>a</sup> <i>A</i> <sub>1ij</sub>	<sup>a</sup> <i>A</i> <sub>1ji</sub>	<sup>a</sup> <i>α</i> <sub>ij</sub>	<sup>a</sup> rmsd (%)
PEG 1500–Na <sub>2</sub> S <sub>2</sub> O <sub>3</sub>	–688.4	4699.7	130.380	–33.450	0.2002	<b>1.78</b>
PEG 1500–water	–3588.9	6709.0	68.071	0.2676	0.4700	
Na <sub>2</sub> S <sub>2</sub> O <sub>3</sub> –water	–117.0	784.61	66.574	128.270	0.2000	
PEG 4000–Na <sub>2</sub> S <sub>2</sub> O <sub>3</sub>	–6730.9	5360.4	–34.810	24.468	0.4700	<b>0.93</b>
PEG 4000–water	–3275.4	5617.0	–17.979	–0.6747	0.2337	
Na <sub>2</sub> S <sub>2</sub> O <sub>3</sub> –water	–144.7	504.9	–31.935	27.961	0.4695	
PEG 6000–Na <sub>2</sub> S <sub>2</sub> O <sub>3</sub>	2761.2	7140.6	–237.000	–0.4501	0.2000	<b>0.96</b>
PEG 6000–water	–2866.3	5243.2	–16.870	–0.3119	0.3075	
Na <sub>2</sub> S <sub>2</sub> O <sub>3</sub> –water	–274.55	–785.9	–31.318	–16.466	0.4514	

<sup>a</sup> In which RMSD is  $\delta_x = 100 \cdot ((\sum_i^M \sum_j^N (x_{ij}^{l,exp} - x_{ij}^{l,calc})^2 + (x_{ij}^{ll,exp} - x_{ij}^{ll,calc})^2) / 2MN)^{1/2}$ , *A*<sub>0ij</sub> and *A*<sub>1ij</sub> are the characteristic parameters of energy of the *i*-*j* interactions, and parameter *α*<sub>ij</sub> is related to the non-randomness of the mixture.

of temperature. On the other hand, TLL increases with the increase in temperature, and this effect is less evident for PEG 6000.

### 3.3. NRTL model

Experimental data were correlated with the non-random two-liquid (NRTL) model on the molar basis [49]. The liquid-liquid equilibrium correlation was made using the estimated molecular energy interaction parameters. The values of the binary interaction parameters obtained for the NRTL model are listed in Table 5 along with the root mean square deviations (RMSD).

As shown in Table 1, the NRTL model was able to represent the phase split over the entire range of compositions analyzed. The mean deviations were found to be < 1.8%. The estimation of the model parameters followed the method described by Stragevitch and d'Ávila [50]. Graphical comparisons between the experimental and calculated data, for all temperatures, are depicted in Figures S1–S3 in the Supplementary Material.

## 4. Conclusion

Liquid-liquid equilibrium data of biphasic aqueous systems formed by PEG and sodium thiosulfate pentahydrate at *T* = (293.15, 303.15 and 313.15) K with *u*(*T*) = 0.05 and under atmospheric pressure were obtained experimentally. Tie line data were verified through equations of Othmer-Tobias and Bancroft indicating the quality of experimental data for both tests. The NRTL model correlated satisfactorily with the experimental data. The effect of the temperature and molecular weight of PEG on the binodal curves were also studied, being demonstrated that biphasic region expands with their increase. On the other hand, temperature affected the slope of the tie lines, but no notable effect was shown for molecular weight of PEG. A comparison between the binodal data of this study and of the literature showed the following order of the salting-out ability for the anions of the salts: C<sub>6</sub>H<sub>5</sub>O<sub>7</sub><sup>3–</sup> (citrate) > S<sub>2</sub>O<sub>3</sub><sup>2–</sup> (thiosulfate) > C<sub>4</sub>H<sub>4</sub>O<sub>6</sub><sup>2–</sup> (tartrate) > KC<sub>4</sub>H<sub>4</sub>O<sub>6</sub><sup>2–</sup> (Ktartrate) > C<sub>4</sub>H<sub>4</sub>O<sub>4</sub><sup>2–</sup> (succinate) > CHO<sup>2–</sup> (formate). This comparison agrees with the values of ( $\Delta G_{hyd}$ ). It was also verified that an increase in the amounts of salt in the global composition is related to greater TLL values for all PEG-salt systems.

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## Appendix A. Supplementary data

Supplementary data related to this article can be found at <https://doi.org/10.1016/j.fluid.2018.07.035>.

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