



## Energy transfer between terbium and europium ions in barium orthosilicate phosphors obtained from sol-gel route



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### ABSTRACT

The present paper reports on the energy transfer mechanism between  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$  in barium orthosilicate obtained from the sol-gel route, when both activators concentration is varied. The synthetic methodology was adjusted to provide high crystalline and monophasic  $\text{Ba}_2\text{SiO}_4$ . In the emission spectra under 250 nm excitation, both  $\text{Eu}^{3+}$  ( $^5\text{D}_0 \rightarrow ^7\text{F}_J$ ) and  $\text{Tb}^{3+}$  ( $^5\text{D}_3 \rightarrow ^7\text{F}_J$  and  $^5\text{D}_4 \rightarrow ^7\text{F}_J$ ) transitions can be observed at low  $\text{Eu}^{3+}$  doping concentrations with an unexpected and intense blue emission from  $\text{Tb}^{3+}$ . However, when the  $\text{Eu}^{3+}$  content is higher than that of the  $\text{Tb}^{3+}$ , just the  $\text{Eu}^{3+}$  emission is noticed. Also, it is possible to tune the phosphor emission from red to pink by varying the  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$  content. From the excitation spectra, we inferred that energy transfer (ET) from  $\text{Tb}^{3+}$  to  $\text{Eu}^{3+}$  occurs at any doping situation, nonetheless, the opposite process happens just when both activators amount is similar. An approach using the  $\text{Tb}^{3+}$  and  $\text{Eu}^{3+}$  lifetimes and the  $\text{Eu}^{3+}$  quantum efficiency confirms this observation, indicating that not only the matrix act as sensitizer to the  $\text{Eu}^{3+}$  ions, but also  $\text{Tb}^{3+}$  ions contribute by increasing the  $\text{Eu}^{3+}$  quantum efficiency in up to 20%. Finally, by using the Van Uitert theory, it was found for this system that the ET between the two rare-earth ions is dominated by the dipole-dipole mechanism.

### 1. Introduction

Rare earth (RE)-doped nanophosphors display unique optical properties that combined with good thermal and chemical stability, make these systems suitable for luminescence and photonic applications [1]. In special, RE-doped barium orthosilicate have been used in solid state lighting devices as white light emitting diode (w-LEDs) [2,3] which are replacing fluorescent and incandescent light sources due to their high energy conversion efficiency resulting in an energy saving, compactness, and long duration time [4,5].  $\text{Eu}^{3+}$  ion, for instance, is an efficient red emitting activator due to its emission lines that arise from the  $^5\text{D}_0$  excited level to the  $^7\text{F}_J$  ( $J = 0, 1, 2, 3, 4, 5, 6$ ) ground levels [6,7]. Also, the relative intensity, position and degenerescence of  $\text{Eu}^{3+}$  transitions are dependent on the host lattice nature, chemical composition and crystalline structure, allowing its use as structural probes [8].  $\text{Tb}^{3+}$ , in turn, has two main emission levels  $^5\text{D}_4$ , and  $^5\text{D}_3$  [9]. The transitions from the first one to the ground  $^7\text{F}_J$  levels result in green emission, while the transitions from the second one is less common, resulting in blue emission, and depend on the  $\text{Tb}^{3+}$  concentration, and on the crystal structure and phonon frequency of the matrix [10].  $\text{Ba}_2\text{SiO}_4$  is an inorganic insulator matrix widely used to host RE

activators due its relative low phonon frequency ( $\sim 900 \text{ cm}^{-1}$ ) and high structural, thermal and electrical stability [11,12]. For the best of your knowledge, no study has been reported about the synthesis of barium orthosilicate simultaneously doped with  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$ , while recently, we reported the synthesis of the  $\text{Eu}^{3+}$ -doped  $\text{Ba}_2\text{SiO}_4$  from the sol gel-route [13]. On the other side, many reports on the synthesis of  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$ -codoped phosphors based on host lattices distinct from  $\text{Ba}_2\text{SiO}_4$  can be found in the literature, aiming application in white LEDs devices [14–18]. As example, M. A. Tshabalala et al. [19] described the solid state synthesis of  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$ -doped strontium orthosilicate and its white emission under UV excitation. However, one of the challenges concerning these codoped phosphors is to understand the energy transfer (ET) mechanism between  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$  ions in order to modulate the phosphor white emission. Indeed, there is a lack in the literature about this kind of approach dealing with ET between these ions specifically in barium orthosilicate matrix. In this paper, we report the synthesis of  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$ -codoped barium orthosilicate phosphor from the sol-gel route, and we propound a detailed interpretation of the ET process by varying the concentration of the two activator ions in order to use  $\text{Tb}^{3+}$ , along with the matrix, as sensitizer for the  $\text{Eu}^{3+}$  emission.

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## 2. Experimental

The Tb<sup>3+</sup> and Eu<sup>3+</sup>-codoped Ba<sub>2</sub>SiO<sub>4</sub> powder samples were synthesized by applying an adapted sol-gel route developed in our research group [13,20]. Tetraethylorthosilicate (TEOS, C<sub>8</sub>H<sub>20</sub>O<sub>4</sub>Si, 99.9%, Fluka), hydrogen peroxide (H<sub>2</sub>O<sub>2</sub>, 36%, Synth), acetic acid (CH<sub>3</sub>COOH, 97%, VETEC), barium acetate (Ba(CH<sub>3</sub>COO)<sub>2</sub>, 99.9%, VETEC), europium oxide (Eu<sub>2</sub>O<sub>3</sub>, 99.99%, Aldrich), hydrochloric acid (HCl, 37%, Sigma), and terbium oxide (Tb<sub>4</sub>O<sub>7</sub>, 99.99%, Aldrich) were used as reactants. Europium acetate (Eu(CH<sub>3</sub>COO)<sub>3</sub>) and terbium chloride (TbCl<sub>3</sub>) solutions were prepared by dissolving the RE oxide in hot acetic acid or hydrochloric acid, respectively. For the complete dissolution of the Tb<sub>4</sub>O<sub>7</sub>, it was necessary the addition of some drops of H<sub>2</sub>O<sub>2</sub>. The xerogel precursors for the Ba<sub>2</sub>SiO<sub>4</sub> powders were synthesized by dissolving stoichiometric amount of Ba(CH<sub>3</sub>COO)<sub>2</sub>, Eu(CH<sub>3</sub>COO)<sub>3</sub> and TbCl<sub>3</sub> in acetic acid (10 mL), aiming to obtain 1.0000 g of Ba<sub>2</sub>Eu<sub>x</sub>Tb<sub>y</sub>SiO<sub>4</sub> powder. Following, TEOS (0.55 M, in isopropyl alcohol) was stoichiometrically added in the solution containing the metal precursors. The solution was kept under magnetic stirring for 4 h (35 °C) until the gel precursor formation. The gel was dried at 120 °C for 2 h, resulting in the xerogel phase. Finally, the xerogel precursor was calcinated at 1100 °C for 2 h with a heating ramp of 10 °C/min in an EDG muffle furnace type, under a circulating air atmosphere, obtaining the phosphor particles. The Eu<sup>3+</sup> and Tb<sup>3+</sup> amounts were isoelectronically varied in order to keep the same overall charge in the system, according to the Ba<sup>2+</sup>, Eu<sup>3+</sup>, Tb<sup>3+</sup> and SiO<sub>4</sub><sup>4-</sup> charges ( $3n_{Eu^{3+}} + 3n_{Tb^{3+}} + 2n_{Ba^{2+}} = +4$ , where  $n_{Ba^{2+}}$ ,  $n_{Tb^{3+}}$  and  $n_{Eu^{3+}}$  are the mol number of Ba<sup>2+</sup>, Tb<sup>3+</sup> and Eu<sup>3+</sup>, respectively). The stoichiometric amounts of Eu<sup>3+</sup>, Tb<sup>3+</sup> and Ba<sup>2+</sup> ions in each phosphor are shown in the Supplementary material, Table ES1, and the samples synthesized are listed in Table 1.

Powder crystalline structure was checked by using a SIEMENS diffractometer model D5000, Cu K $\alpha$  radiation ( $\lambda = 1,5405 \text{ \AA}$ ), a  $2\theta$  range of 20–45°, an increment of 0.02° and integration time of 1 s. The samples were also characterized by scanning electron microscopy (SEM) using a Carls Zeiss model EVO LS15 microscope with a detector of secondary electrons (SE) in high vacuum and constant temperature. Finally, photoluminescence measurements at room temperature were carried out in a Horiba JobinYvon spectrometer Fluorolog-3 with a Xe lamp (450 W) source with double excitation monochromator. Emission lifetime was evaluated using a phosphorimeter equipped with Xe (5 J/pulse) lamp.

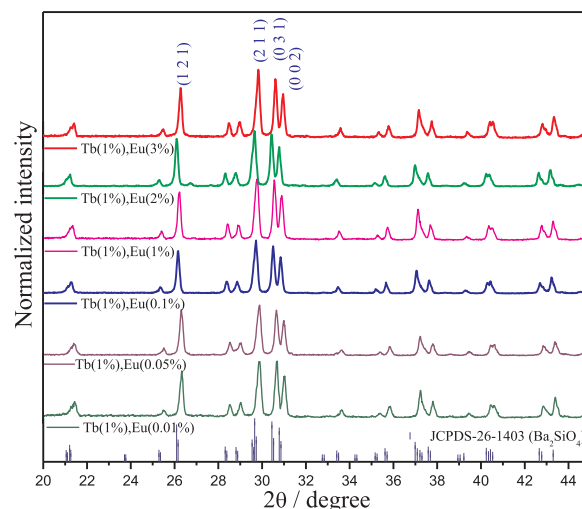
**Table 1**

Tb/Eu emission rate, and critical distance ( $R_c$ ) between Eu<sup>3+</sup> and Tb<sup>3+</sup> ions.

Tb/ Eu (%)	Tb/Eu emission rate <sup>a</sup>	$R_c$ Eu-Eu/ $\text{\AA}^b$	$R_c$ Tb-Tb/ $\text{\AA}^b$	$R_c$ Eu-Tb/ $\text{\AA}^b$
2/2	1.19	8.54	8.54	6.78
2/0.1	0.09	23.5	8.62	8.49
1/3	–	7.46	10.8	6.78
1/2	0.58	8.58	10.8	7.50
1/1	0.92	8.67	10.9	8.63
1/0.1	0.48	23.5	10.9	10.6
1/0.05	0.59	29.7	10.9	10.7
1/0.01	0.34	50.7	10.9	10.9
0.5/4	–	6.76	13.5	6.50
0.5/1	1.13	10.90	13.7	9.52
0.5/0.5	0.96	13.7	13.7	10.9
0.1/4	–	6.77	23.2	10.4

<sup>a</sup> The Tb/Eu emission rate parameter was determined by the rate between the sum of the integrated area below the Terbium and Europium transitions in the emission spectra under excitation at 250 nm.

<sup>b</sup> The Ln-Ln distance was calculated considering the Ln<sup>3+</sup> concentration in Eq. (2).



**Fig. 1.** Powder X-ray diffractograms of the phosphors doped with 1% of Tb<sup>3+</sup> and varying the Eu<sup>3+</sup> content.

## 3. Results

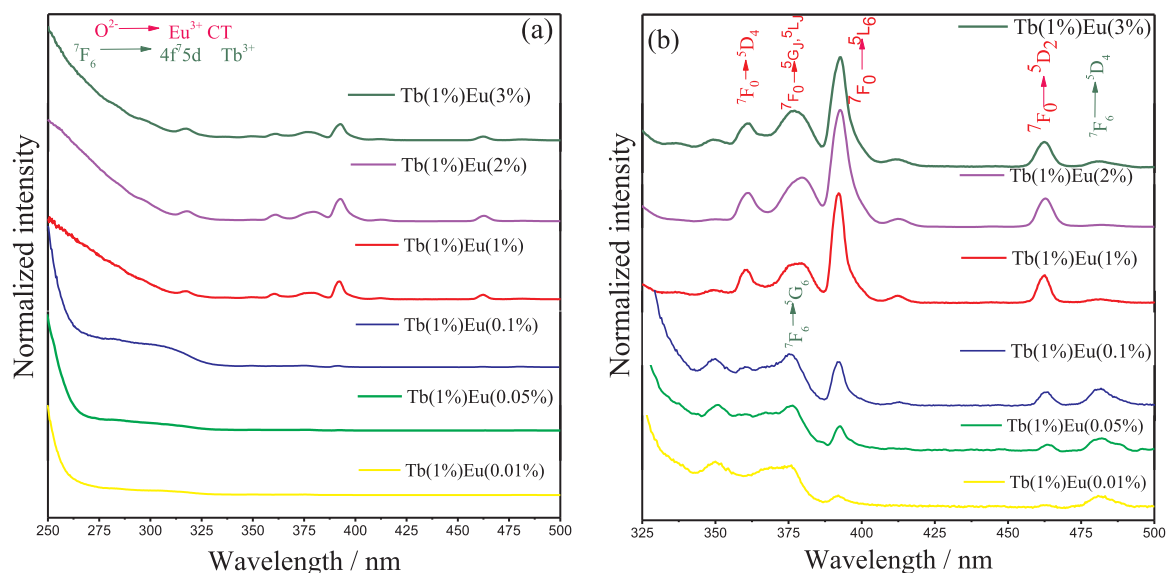
X-ray diffraction (XRD) patterns of representative samples are shown in Fig. 1 and for all other samples, the results are shown in Fig. S1, Supplementary material. XRD data confirm that the phosphors obtained by the sol-gel route at 1100 °C are crystalline, with orthorhombic crystal system (JCPDS 26–1403 card), and  $P_{man}$  space group. Regarding the limit of detection of this technique, there is no evidence of Eu<sub>2</sub>O<sub>3</sub> and Tb<sub>4</sub>O<sub>7</sub> formation, which corroborate for the fact that both activator ions are inserted into the Ba<sub>2</sub>SiO<sub>4</sub> lattice and can occupy two different sites, one with coordination number (CN) 9 and another with CN 10 [21]. In addition, the mean crystallite size calculated via Scherrer's method [22], varied from 49 to 76 nm for all produced samples. The full data are included in the Supplementary material, Table ES2. Moreover, it is clear that the increase of the Eu<sup>3+</sup> concentration in relation to the Tb<sup>3+</sup> leads to an increase in the mean diameter of the crystallites.

SEM images of some representative phosphors are shown in Fig. S2, in the Supplementary material. The observed particles are irregular in shape and size, yet the mean size was estimated at about 330 nm, and some particles are spherical while others are ellipsoidal shaped.

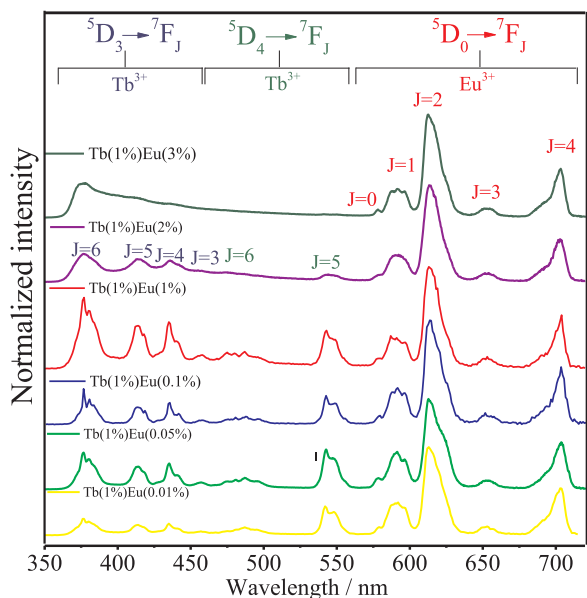
Fig. 2 exhibits the photoluminescence excitation spectra of the codoped phosphors monitoring the <sup>5</sup>D<sub>0</sub>→<sup>7</sup>F<sub>2</sub> transition of Eu<sup>3+</sup> at 612 nm. The most intense band observed in the excitation spectra at high energies is assigned to both Tb<sup>3+</sup> <sup>7</sup>F<sub>6</sub>→<sup>4</sup>f<sup>7</sup>5d transition and O<sup>2-</sup>→Eu<sup>3+</sup> charge transfer. The magnification of the range within 325–500 nm shows the Eu<sup>3+</sup> and the Tb<sup>3+</sup> *f-f* transitions in all spectra, indicating that the Eu<sup>3+</sup> emission arises from both RE<sup>3+</sup> excitation. This observation lead us to conclude that the ET from Tb<sup>3+</sup> to Eu<sup>3+</sup> ions (Tb<sup>3+</sup>→Eu<sup>3+</sup>) is taking place in all phosphors. The ET between the two ions is favored because the energies of the <sup>5</sup>D<sub>3</sub> (26,402 cm<sup>-1</sup>) and <sup>5</sup>D<sub>4</sub> (20,640 cm<sup>-1</sup>) [23] levels of Tb<sup>3+</sup> ions, and the <sup>5</sup>D<sub>0</sub> (17,280 cm<sup>-1</sup>), <sup>5</sup>D<sub>1</sub> (18,973 cm<sup>-1</sup>), <sup>5</sup>D<sub>2</sub> (21,445 cm<sup>-1</sup>), and <sup>5</sup>D<sub>3</sub> (24,335) [6] levels of Eu<sup>3+</sup> ions are close enough to allow the resonance between them.

In the emission spectra recorded with excitation wavelength fixed at 250 nm, Fig. 3, both ions are excited via Tb<sup>3+</sup> <sup>7</sup>F<sub>6</sub>→<sup>4</sup>f<sup>7</sup>5d and O<sup>2-</sup>→Eu<sup>3+</sup> transitions, resulting in green and blue emission from Tb<sup>3+</sup>, and red emission from Eu<sup>3+</sup>. When the Eu<sup>3+</sup> content is much higher than that of Tb<sup>3+</sup>, the Tb<sup>3+</sup> emission is neglected, just the matrix intrinsic emission is observed in the blue range (see the matrix intrinsic luminescent profile in Fig. S4).

The Eu<sup>3+</sup> red emission comes from the <sup>5</sup>D<sub>0</sub>→<sup>7</sup>F<sub>0,1,2,3,4</sub> transitions, attributed to Eu<sup>3+</sup> ions occupying low-symmetry sites [24]. The Tb<sup>3+</sup>



**Fig. 2.** Excitation spectra of  $\text{Ba}_2\text{SiO}_4:\text{Tb}^{3+},\text{Eu}^{3+}$  samples measured at room temperature. The emission wavelength was fixed in the  $\text{Eu}^{3+}$  emission at 612 nm (a). Magnification of the range between 325 and 500 nm, where  $\text{Tb}^{3+}$  transitions assignments are shown in green and the  $\text{Eu}^{3+}$  ones in red (b). The excitation spectra of the other phosphors are shown in Fig. ES3.



**Fig. 3.** Emission spectra of  $\text{Ba}_2\text{SiO}_4:\text{Tb}^{3+},\text{Eu}^{3+}$  samples measured at room temperature. The emission spectra of the other phosphors are shown in Fig. S5. The excitation wavelength was fixed in 250 nm.  $\text{Tb}^{3+}$  transitions assignments are shown in green and blue and  $\text{Eu}^{3+}$  in red.

blue emission, in turn, is assigned to transitions from the  $^5\text{D}_3$  excited level while the green emission comes from the  $^5\text{D}_4$  level to the  $^7\text{F}_J$  ground level. Usually, the  $\text{Tb}^{3+}$  blue emission is very weak due to the cross relaxation mechanism involving the  $^5\text{D}_3$  and  $^5\text{D}_4$  levels which quenches the  $^5\text{D}_3$  emission (see Eq. (1)) [25]. However, when the  $\text{Tb}^{3+}$  concentration is low, the Tb-Tb distance is long enough to inhibit the cross relaxation, favoring the blue emission from the  $^5\text{D}_3$  level. In literature, the  $\text{Tb}^{3+}$  blue emission is reported for concentration less than 0.01 at% [10,25], but in the present case, the intense blue emission begins to take place at  $\text{Tb}^{3+}$  concentrations relatively high (~1%). Also, host matrix with phonon energy lower than  $1000\text{ cm}^{-1}$  favors the  $^5\text{D}_3$  blue emission due to the absence of multi phonon relaxation [26]. The phonon energy in the barium orthosilicate is  $900\text{ cm}^{-1}$  [26], then the multiphonon relaxation process that can compete with the  $^5\text{D}_3$

radiative emission is unlikely to take place, since the multiphonon mechanism is limited by the coupling of a maximum of 4 or 5 phonons [26].

$$\text{Tb}^{3+}(^5\text{D}_3) + \text{Tb}^{3+}(^7\text{F}_6) \rightarrow \text{Tb}^{3+}(^5\text{D}_4) + \text{Tb}^{3+}(^7\text{F}_0) \quad (1)$$

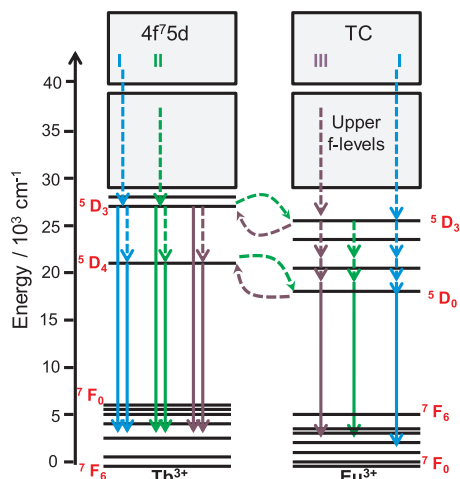
The rate between terbium and europium emission integrated areas for all phosphors is listed in Table 1. For the samples doped with 1% of  $\text{Tb}^{3+}$ , the increase of  $\text{Eu}^{3+}$  concentration leads to an increment in the  $\text{Tb}^{3+}$  emission up to 1% of  $\text{Eu}^{3+}$ . Then, the  $\text{Eu}^{3+}$  emission overcomes the  $\text{Tb}^{3+}$  one. This behavior leads us to conclude that ET from  $\text{Eu}^{3+}$  to  $\text{Tb}^{3+}$  ( $\text{Eu}^{3+} \rightarrow \text{Tb}^{3+}$ ) dominates the ET up to 1% of  $\text{Eu}^{3+}$ , and at higher  $\text{Eu}^{3+}$  concentrations, on the other side, the  $\text{Tb}^{3+} \rightarrow \text{Eu}^{3+}$  ET is the main process. The same profile is observed for samples doped with 0.5% of  $\text{Tb}^{3+}$ .

The  $\text{Eu}^{3+} \rightarrow \text{Tb}^{3+}$  ET mechanism proposition is indorsed by analyzing the excitation spectra monitoring the  $\text{Tb}^{3+} ^5\text{D}_4 \rightarrow ^7\text{F}_5$  emission (Fig. S6), where the  $\text{Eu}^{3+} ^7\text{F}_0 \rightarrow ^5\text{L}_6$  transition is observed for the sample doped with 1% of  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$ , indicating that  $\text{Tb}^{3+}$  emission can be achieved via  $\text{Eu}^{3+}$  excitation. For the samples with low  $\text{Eu}^{3+}$  concentrations, the  $\text{Eu}^{3+}$  excitation cannot be observed because the  $\text{Ba}_2\text{SiO}_4$  intrinsic excitation overcomes the  $\text{Tb}^{3+}$  lines.

An extrapolation of  $\text{Eu}^{3+}$ -doping in relation to the  $\text{Tb}^{3+}$  concentration (sample doped with 0.1% of  $\text{Tb}^{3+}$  and 4% of  $\text{Eu}^{3+}$ ) shows that the  $\text{Tb}^{3+}$  emission is quenched when the  $\text{Eu}^{3+}$  content is too high. In addition, when both  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$  doping are the same, the  $\text{Tb}^{3+}$  and  $\text{Eu}^{3+}$  emission intensity are similar, probably because the  $\text{Eu}^{3+} \rightarrow \text{Tb}^{3+}$  and  $\text{Tb}^{3+} \rightarrow \text{Eu}^{3+}$  ET rates are too close in these cases. Therefore, the  $\text{Eu} \rightarrow \text{Tb}$  ET occurs just when both the  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$  content are close.

Fig. 4 shows some propositions of ET mechanisms between  $\text{Tb}^{3+}$  and  $\text{Eu}^{3+}$  in  $\text{Ba}_2\text{SiO}_4$  host. In the mechanism I, both  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$  emit under 250 nm excitation. In the mechanism II, the ET from  $\text{Tb}^{3+}$  to  $\text{Eu}^{3+}$  is shown and occurs for all samples, dominating the ET profile at high  $\text{Eu}^{3+}$  concentrations. In the case of mechanism III, the ET from  $\text{Eu}^{3+}$  to  $\text{Tb}^{3+}$  is represented and dominate the ET between the RE ions just for samples with low  $\text{Eu}^{3+}$  doping concentrations.

Usually, the energy transfer among RE ions involves radiation reabsorption, exchange or multipole-multipole interactions [27]. However, in the present system, the radiation reabsorption mechanism is unlikely to take place because it requires a wide overlap between the donor emission and acceptor excitation spectra, which is not observed



**Fig. 4.** Energy transfer mechanisms between  $\text{Tb}^{3+}$  and  $\text{Eu}^{3+}$  ions (dashed arrows: non-radiative transitions; solid line arrows: radiative transitions, curved lines: energy transfer). The mechanism I (blue lines) represent the emission from both RE ions under excitation at 250 nm without energy transfer. The mechanism II (green lines) represent the  $\text{Tb}^{3+} \rightarrow \text{Eu}^{3+}$  ET and the emission from both RE ions. The mechanism III (purple lines) represent the  $\text{Eu}^{3+} \rightarrow \text{Tb}^{3+}$  ET and both RE emissions. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

in this system. Considering the exchange coupling possibility, it is necessary to evaluate the critical distance ( $R_c$ ) between the donor and acceptor because this mechanism is limited by 4 Å to allow an orbital overlap [28]. In this context, the critical distance was determined by using Eq. (2) [29], where  $n_A$  is equal to  $(x \cdot n)/V$ ,  $V$  is the unit cell volume ( $V = 444.257 \text{ \AA}^3$ , from the JCPDS-26-1403 card),  $x$  is the dopant concentration, and  $n$  is the  $\text{Ba}^{2+}$  mol number per unit cell ( $n = 8$  from the JCPDS-26-1403 card). The estimated critical distance is shown in Table 1.

$$R_c = \left[ \frac{3}{4\pi n_A} \right]^{1/3} \quad (2)$$

The calculated  $R_c$  indicates that an exchange interaction is unlikely to take place since the values are higher than 4 Å. Thus, the multipolar interaction must be the main factor that contributes to the energy transfer mechanism.

In order to investigate the dominant multipolar mechanism responsible for the ET between  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$  ions, it was used the theoretical model developed by Van Uitert [30] showed in the Eq. (3), where  $x$  is the acceptor concentration,  $I$  is the emission intensity obtained from the emission spectra, and  $\beta$  is a constant. In this model,  $\theta$  is a function of the dominant ET mechanism between the donor and acceptor species. Electric dipole–dipole (D–D) interactions are represented by  $\theta = 6$ , electric dipole–quadrupole (D–Q) interactions correspond to  $\theta = 8$  and electric quadrupole–quadrupole (Q–Q) interactions, in turn, are represented by  $\theta = 10$ . In Fig. 5 it is plotted the  $\log(x)$  versus  $\log(I/x)$ , where the intensity was fixed in both  $\text{Tb}^{3+} \ ^5\text{D}_4 \rightarrow \ ^7\text{F}_5$  and  $\text{Eu}^{3+} \ ^5\text{D}_0 \rightarrow \ ^7\text{F}_2$  transitions. The  $\theta$  values deduced from the fitting plots monitoring the emission of both RE ions are closer to 6, suggesting that D–D interaction are the main contribution for the ET between  $\text{Tb}^{3+}$  and  $\text{Eu}^{3+}$  ions in the  $\text{Ba}_2\text{SiO}_4$  matrix.

$$\frac{I}{x} = [1 + \beta(x)^{\theta/3}]^{-1} \quad (3)$$

The CIE chromaticity coordinates obtained for all phosphors are presented in the diagram in Fig. 6. When the  $\text{Tb}^{3+}$  concentration is fixed at 1%, the emission moves to pink, when the  $\text{Eu}^{3+}$  concentration increase from 0.01 up to 1%, then goes back to red. This occurs because the  $\text{Tb}^{3+}$  emission is favored up to 1% of  $\text{Eu}^{3+}$ , from then on, the  $\text{Eu}^{3+}$  emission overcomes the  $\text{Tb}^{3+}$  emission. Samples with equal RE

concentration emit near to pink, since both red and blue emissions of  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$  respectively have similar intensities. The phosphors with low  $\text{Tb}^{3+}$  concentration emit near to pink due to the blue contribution of the matrix emission. Thus, the emission color is tunable by varying the dopant concentration.

The Judd-Ofelt intensity parameters were evaluated from the emission spectra data and its values are summarized in Table 2. In this theory, the  $\ ^5\text{D}_0 \rightarrow \ ^7\text{F}_2$  and  $\ ^5\text{D}_0 \rightarrow \ ^7\text{F}_4$  transitions are directly correlated to  $\Omega_2$  and  $\Omega_4$  intensity parameters, which can be calculated from the integrated areas below the transitions  $\ ^5\text{D}_0 \rightarrow \ ^7\text{F}_1$ ,  $\ ^5\text{D}_0 \rightarrow \ ^7\text{F}_2$ , and  $\ ^5\text{D}_0 \rightarrow \ ^7\text{F}_4$ , as shown in Eqs. (4) and (5) [32].

$$A_{0-\lambda} = A_{0-j} = A_{01} \frac{I_{0-j} h\nu_{0-1}}{I_{0-1} h\nu_{0-j}} \quad (4)$$

$$\sum_{\lambda=2,4} \Omega_{\lambda} \langle \ ^5\text{D}_0 \rangle^2 = A_{01} \frac{I_{0-j} h\nu_{0-1}}{I_{0-1} h\nu_{0-j}} \frac{3hc^3 4\epsilon_0}{64\pi^3 e^2} \frac{1}{\nu_{\lambda}^3 x} \quad (5)$$

Where the term  $\langle \ ^5\text{D}_0 \rangle^2$  represent the square reduced matrix elements which is equal to 0.0032 and 0.0023 for  $\Omega_2$  and  $\Omega_4$ ; respectively [32];  $e$ ,  $h$ ,  $\epsilon_0$  and  $c$  are the electron charge, the Planck's constant, the vacuum permittivity constant; and the speed of light in vacuum, respectively;  $A_{01}$  is equal to  $14.65 \cdot n$  [3] ( $n$  is the refractive index considered in this case as 1.7 [13]) and corresponds to the Einstein's coefficient for spontaneous emission [33];  $I_{0-j}$  is the integrated area under the respective  $\ ^5\text{D}_0 \rightarrow \ ^7\text{F}_j$  transitions; and  $x$  is given by  $n(n^2 + 2)^2/9$  and corresponds to the Lorentz local field correction.

The relatively low values of  $\Omega_4$  compared to other systems [34,35] indicate that the chemical environment around  $\text{Eu}^{3+}$  is low polarizable, suggesting a low covalence degree of the Eu-O bond, since the  $\Omega_4$  intensity parameter is more sensitive to changes in the electron density around the  $\text{Eu}^{3+}$ , caused by variations in the Eu-O bond distance [36]. On the other hand, the  $\Omega_2$  value is more sensitive to changes in the  $\text{Eu}^{3+}$  site symmetry related to angular distortions in the Eu-O bonds [37]. The relatively low values of  $\Omega_2$  intensity parameters compared to other systems [34,35] indicate that the environment around the  $\text{Eu}^{3+}$  ions is relatively symmetric. This occurs because the doping does not cause strong distortions in the  $\text{Eu}^{3+}$  sites [13]. Also, there is a tendency of enhancement for the  $\Omega_2$  values when the  $\text{Eu}^{3+}$  concentration increase, showing that the  $\text{Eu}^{3+}$  local symmetry is lowered. The  $\ ^5\text{D}_0 \rightarrow \ ^7\text{F}_2$  is considered hypersensitive to the environment, and its intensity increase as the symmetry around the  $\text{Eu}^{3+}$  ion decrease.

Emission lifetime ( $\tau$ ) data shown in Table 2 were obtained by monitoring the  $\text{Eu}^{3+} \ ^5\text{D}_0$  excited level and  $\text{Tb}^{3+} \ ^5\text{D}_3$  and  $\ ^5\text{D}_4$  levels. The obtained curves are shown in Fig. S7 and were best adjusted by applying a mono-exponential fit. The  $\text{Tb}^{3+}$  lifetime values were used to estimate the  $\text{Tb} \rightarrow \text{Eu}$  ET efficiency by applying Eq. (6) [38], where  $\tau_1$  is the lifetime value for the codoped sample and  $\tau_{10}$  is the lifetime value for the  $\text{Tb}^{3+}$  single doped samples. The emission spectra for the single doped  $\text{Ba}_2\text{SiO}_4:\text{Tb}^{3+}$  (2%, 1%, 0.5% and 0.1%-doped) are shown in Fig. S7 and the ET efficiencies are shown in Table 2.

$$\eta_{\text{Tb} \rightarrow \text{Eu}} = 1 - \frac{\tau_1}{\tau_{10}} \quad (6)$$

From Table 2, the  $\text{Tb} \rightarrow \text{Eu}$  ET efficiency increase in the samples that have  $\text{Eu}^{3+}$  content much lower or higher than that of  $\text{Tb}^{3+}$ , showing that the  $\text{Tb} \rightarrow \text{Eu}$  ET prevails in relation to the opposite process. In these cases, the ET efficiency value from the  $\text{Tb}^{3+} \ ^5\text{D}_3$  level is higher than that from the  $\ ^5\text{D}_4$  one, showing that the  $\text{Tb} \rightarrow \text{Eu}$  ET occurs mainly via the  $\text{Tb}^{3+} \ ^5\text{D}_3$  level. As expected from the emission spectra, when the  $\text{Tb}^{3+}$  content is much lower than that of  $\text{Eu}^{3+}$  ( $\text{Tb}(0.5)\text{Eu}(4)$  and  $\text{Tb}(0.1)\text{Eu}(4)$ ), the ET efficiency from both  $\ ^5\text{D}_3$  and  $\ ^5\text{D}_4$  levels are 100%, indicating that this is the best condition to improve the  $\text{Eu}^{3+}$  efficiency. This efficient  $\text{Tb} \rightarrow \text{Eu}$  ET can also be evidenced by the increase of the  $\text{Eu}^{3+} \ ^5\text{D}_0$  lifetime values for these samples when compared to the single doped  $\text{Ba}_2\text{SiO}_4:\text{Eu}^{3+}$  (compare in Table 1 the lifetime values for the samples single-doped or codoped with 4% of  $\text{Eu}^{3+}$ ).

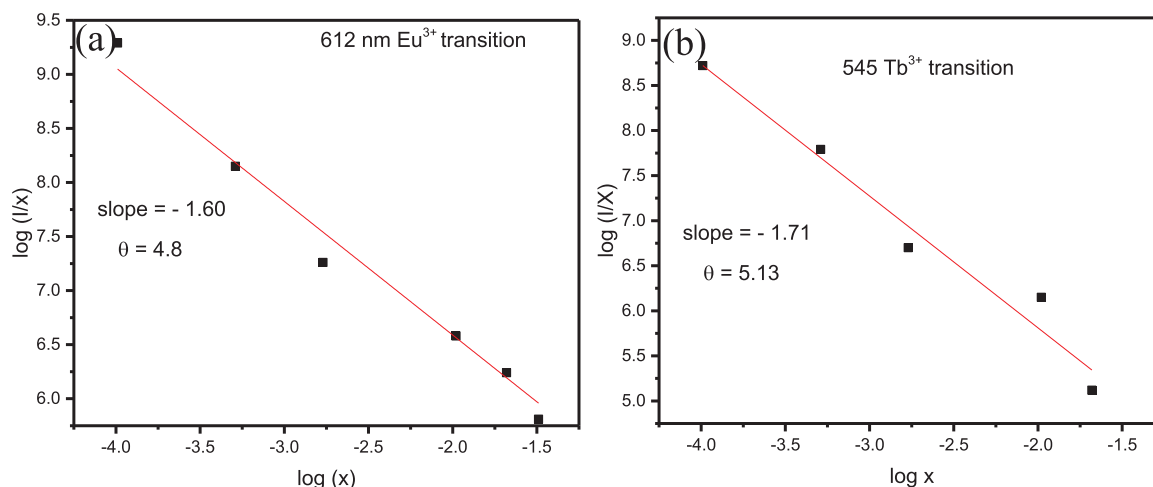


Fig. 5. Linear fitting of  $\log(x)$  versus  $\log(I/x)$  for  $\text{Ba}_2\text{SiO}_4:\text{Eu}^{3+}(x\%),\text{Tb}^{3+}(1\%)$  phosphors considering the emission intensity at (a) 612 nm and (b) 545 nm.

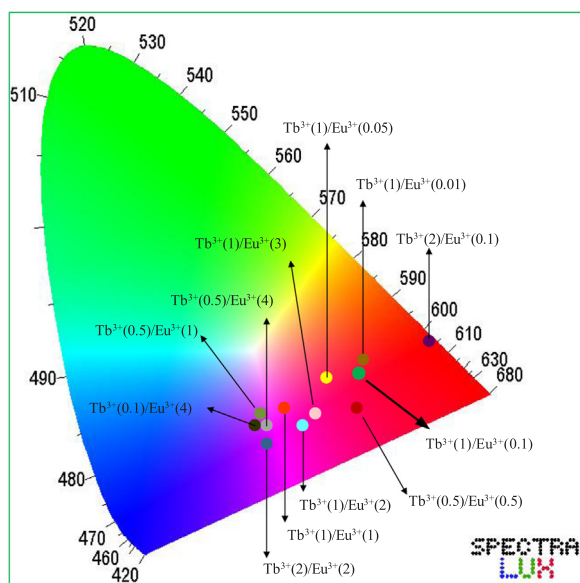


Fig. 6. CIE chromaticity diagram for the  $\text{Tb}^{3+}$  and  $\text{Eu}^{3+}$ -codoped  $\text{Ba}_2\text{SiO}_4$  obtained from Spectra Lux software [31], and the emission spectra collected under 250 nm excitation measured at room temperature.

When the  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$  contents are similar (samples doped with  $\text{Tb}(1)\text{Eu}(1)$ ,  $\text{Tb}(0.5)\text{Eu}(0.5)$ ,  $\text{Tb}(2)\text{Eu}(2)$  and  $\text{Tb}(0.5)\text{Eu}(1)$ ), the  $\text{Tb} \rightarrow \text{Eu}$  ET efficiency for the  $^5\text{D}_3$  level is lower than that of the others, and the ET efficiency from the  $^5\text{D}_4$  level is higher than 100% or very low. These results show that in the  $^5\text{D}_3$  level, the  $\text{Eu} \rightarrow \text{Tb}$  ET is more efficient for the  $^5\text{D}_3$  level population in relation to the other samples, and as consequence, decrease the  $\text{Tb} \rightarrow \text{Eu}$  ET efficiency. Yet considering the  $^5\text{D}_4$  level, a  $\text{Tb} \rightarrow \text{Eu}$  ET efficiency higher than 100% indicates that the opposite process is the main ET process, contributing to the population of the  $^5\text{D}_4$  level and its lifetime value increase. Also, in some cases, a low  $^5\text{D}_4$   $\text{Tb} \rightarrow \text{Eu}$  ET efficiency is an indicative that the opposite ET process is dominating. In this context, the  $\text{Eu} \rightarrow \text{Tb}$  ET occurs mainly via the  $^5\text{D}_4$  level.

The  $\text{Eu}^{3+}$   $^5\text{D}_0$  lifetime values were used to estimate the  $\text{Eu}^{3+}$  quantum efficiency ( $\eta_{\text{Eu}}$ ) also shown in Table 2. The quantum efficiency is the greatness that correlate the radiative ( $A_{\text{rad}}$ ) and the non-radiative ( $A_{\text{nrad}}$ ) contributions from an emitting level (Eq. (7)) [32].

$$\eta = \frac{A_{\text{rad}}}{A_{\text{rad}} + A_{\text{nrad}}} \quad (7)$$

The  $A_{\text{rad}}$  contributions are calculated by the main radiative contributions related to the  $^5\text{D}_0 \rightarrow ^7\text{F}_1$   $\text{Eu}^{3+}$  transitions, as shown in Eq. (8) [32]. Yet, the  $A_{\text{nrad}}$  values are determined directly from the lifetime values, as represented in Eq. (9) [32].

$$A_{\text{rad}} = \sum^J A_{0-j} \quad (8)$$

$$A_{\text{total}} = \frac{1}{\tau} = A_{\text{rad}} + A_{\text{nrad}} \quad (9)$$

For samples doped with 1% of  $\text{Tb}^{3+}$ , the  $\eta_{\text{Eu}}$  decrease when the  $\text{Eu}^{3+}$  concentration increase up to 2%, from then on, the  $\eta_{\text{Eu}}$  has an increment. The reduction of  $\eta_{\text{Eu}}$  is due to the  $\text{Eu}^{3+} \rightarrow \text{Tb}^{3+}$  ET that overcomes the opposite process in these samples, as previously discussed, decreasing the population of  $\text{Eu}^{3+}$   $^5\text{D}_0$  level. However, as the  $\text{Eu}^{3+} \rightarrow \text{Tb}^{3+}$  ET is not efficient at high  $\text{Eu}^{3+}$  doping concentration, the  $\text{Tb}^{3+} \rightarrow \text{Eu}^{3+}$  ET is the dominant process and, as consequence, increase the population of the  $\text{Eu}^{3+}$   $^5\text{D}_0$  level. A similar profile is observed for samples doped with 0.5% of  $\text{Tb}^{3+}$ .

The  $\text{Tb}^{3+}$  ions are acting as sensitizers for the  $\text{Eu}^{3+}$  ions in some specific conditions. Recently, we reported the  $\eta_{\text{Eu}}$  for the  $\text{Eu}^{3+}$  4%-doped sample as 68.2%, as shown in Table 2 [13]. However, when we doped this sample with 0.5% or 0.1% of  $\text{Tb}^{3+}$ , the  $\eta_{\text{Eu}}$  increase to 77.9% and 88.9%, respectively, enhancing in 20% the  $\text{Eu}^{3+}$  quantum efficiency. This occurs because the  $\text{Tb}^{3+} \rightarrow \text{Eu}^{3+}$  ET is high and the  $\text{Tb}^{3+}$  ions act as sensitizers to the  $\text{Eu}^{3+}$  ions, increasing the  $^5\text{D}_0$  level population and as consequence, enhances the  $\text{Eu}^{3+}$  radiative rate, and its quantum efficiency.

#### 4. Conclusions

An energy transfer approach between  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$  ions in monophasic  $\text{Ba}_2\text{SiO}_4$  matrix successfully prepared by the sol-gel route was proposed. Both  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$  emissions could be detected under 250 nm excitation, with an unexpected intense  $\text{Tb}^{3+}$  blue emission from the  $^5\text{D}_3$  level at relatively high  $\text{Tb}^{3+}$  concentration. However, at relatively high  $\text{Eu}^{3+}$  concentrations, the  $\text{Tb}^{3+}$  emission was quenched. It was possible to tune the phosphor emission from red to pink by varying the  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$  content. Considering all doping studied combinations, the energy transfer from  $\text{Tb}^{3+}$  to  $\text{Eu}^{3+}$  ions is taking place in all samples, but the inverse process only dominates when both  $\text{Tb}^{3+}$  and  $\text{Eu}^{3+}$  content are similar. The  $\text{Tb} \rightarrow \text{Eu}$  ET occurs mainly from the  $\text{Tb}^{3+}$   $^5\text{D}_3$  level to the  $\text{Eu}^{3+}$  excited levels but the  $\text{Eu} \rightarrow \text{Tb}$  ET occurs mainly from the  $\text{Eu}^{3+}$  excited levels to the  $\text{Tb}^{3+}$   $^5\text{D}_3$  one. Also, when the  $\text{Eu}^{3+}$  content is much higher than the  $\text{Tb}^{3+}$  concentration, the  $\text{Eu}^{3+}$  quantum efficiency increase, due to the  $\text{Tb}^{3+} \rightarrow \text{Eu}^{3+}$  ET, showing that

**Table 2**

Tb→Eu ET efficiency for all codoped samples (the  $\eta_{\text{Tb} \rightarrow \text{Eu}}(^5\text{D}_3)$  and the  $\eta_{\text{Tb} \rightarrow \text{Eu}}(^5\text{D}_4)$  correspond to the ET from the  $\text{Tb}^{3+} ^5\text{D}_3$  and  $^5\text{D}_4$  levels to the  $\text{Eu}^{3+}$  levels, respectively),  $\text{Tb}^{3+} ^5\text{D}_3$  ( $\tau_{\text{Tb} ^5\text{D}_3}$ ) and  $^5\text{D}_4$  ( $\tau_{\text{Tb} ^5\text{D}_4}$ ) lifetime values,  $\text{Eu}^{3+}$  experimental Judd-Ofelt intensity parameters ( $\Omega_2, \Omega_4$ ),  $\text{Eu}^{3+} ^5\text{D}_0$  lifetime values ( $\tau_{\text{Eu}}$ ), and  $\text{Eu}^{3+}$  quantum efficiency ( $\eta_{\text{Eu}}$ ) for the prepared phosphors.

Tb/Eu (%)	$\eta_{\text{Tb} \rightarrow \text{Eu}}(^5\text{D}_3) / \%$	$\eta_{\text{Tb} \rightarrow \text{Eu}}(^5\text{D}_4) / \%$	$\tau_{\text{Tb} ^5\text{D}_3} / \text{ms}$	$\tau_{\text{Tb} ^5\text{D}_4} / \text{ms}$	$\Omega_2 / \text{pm}$	$\Omega_4 / \text{pm}$	$\tau_{\text{Eu}} / \text{ms}$	$\eta_{\text{Eu}} / \%$
2/2	78	108	0.43	1.53	5.59	4.80	0.73	33.8
2/0.1	82	12	0.36	1.24	4.66	4.69	1.36	56.1
1/3	100 <sup>a</sup>	100 <sup>a</sup>	- <sup>b</sup>	- <sup>b</sup>	5.69	5.18	0.99	46.7
1/2	100 <sup>a</sup>	100 <sup>a</sup>	- <sup>b</sup>	- <sup>b</sup>	5.81	5.22	0.57	27.3
1/1	91	8	0.20	1.26	5.30	4.74	0.83	37.5
1/0.1	91	17	0.20	1.14	4.98	4.96	1.28	55.4
1/0.05	92	12	0.18	1.21	4.57	4.60	1.22	49.6
1/0.01	100	12	- <sup>b</sup>	1.22	4.65	4.90	1.49	61.1
0.5/4	100 <sup>a</sup>	100 <sup>a</sup>	- <sup>b</sup>	- <sup>b</sup>	5.90	4.57	1.67	77.9
0.5/1	90	136	0.27	1.80	5.11	4.40	1.26	54.4
0.5/0.5	84	114	0.43	1.51	5.25	3.90	1.37	58.7
0.1/4	100 <sup>a</sup>	100 <sup>a</sup>	- <sup>b</sup>	- <sup>b</sup>	5.74	4.25	1.97	88.9
0/4 [13]	-	-	-	-	6.20	6.10	1.34	68.2
0/3 [13]	-	-	-	-	6.20	7.20	1.29	58.8
0/2 [13]	-	-	-	-	6.40	5.60	1.11	55.6
0/1 [13]	-	-	-	-	5.90	5.90	1.33	66.5
2/0	-	-	1.92	1.41	-	-	-	-
1/0	-	-	2.21	1.37	-	-	-	-
0.5/0	-	-	2.71	1.32	-	-	-	-
0.1/0	-	-	3.33	1.31	-	-	-	-

<sup>a</sup> For the samples that do not have  $^5\text{D}_3$  and  $^5\text{D}_4$  lifetime values, the Tb→Eu ET efficiency was considered as 100%.

<sup>b</sup> Some samples do not shown  $\text{Tb}^{3+}$  emission and as consequence do not have lifetime values.

$\text{Tb}^{3+}$  ions is acting as sensitizer to  $\text{Eu}^{3+}$  ions. Finally, the energy transfer between the doping ions is dominated by the dipole-dipole multipolar interactions.

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## Conflicts of interest

There are no conflicts to declare.

## Appendix A. Supporting information

Supplementary data associated with this article can be found in the online version at [doi:10.1016/j.jlumin.2018.03.057](https://doi.org/10.1016/j.jlumin.2018.03.057).

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